

# COMPARATIVE STUDY ON ARTIFICIAL NEURAL NETWORKS ADALINE, MADALINE AND HEBB'S

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**Abstract:** In many real-world applications, we want our computers to perform complex pattern recognition problems, such as the one just termed. Since our systems are obviously not suited to this type of problem, we therefore borrow features from the physiology of the brain as the basis for our new processing models. Hence, the technology is known as artificial neural systems (ANS) technology, or simply neural networks. Various algorithms are used for the analysis of artificial neural networks. In this paper we are investigating different algorithms used in artificial neural networks and the applications of ANS.

**Keywords:** Artificial Intelligence, Machine Learning, Algorithms, Neural Computing, Pattern Recognition

## I. INTRODUCTION

Artificial neuron networks are the computational model based on the structure and functions of biological neural networks. These crude electronic models basically learn from the experiences and it is very good at a wide variety of problems, most of which involve finding trends in large quantities of data. These biologically methods of computing are assumed to be the next most important improvement in the computing industry. There are many algorithms used for analysing the artificial network. This paper describes and examines the various algorithms used in the artificial neural network.

## II. PROBLEM STATEMENT

- The perceptrons were not capable of implementing certain elementary functions like XOR
- Evaluates Performance of learning algorithm
- A comparative study of learning techniques as the Adaline, Madaline and Hebb's.
- We will conclude on an algorithm that is better for learning techniques.

## III. PROPOSED ALGORITHM

### A) THE ADALINE (*Adaptive Linear Neuron or Adaptive Linear Element*)

The Adaline is a single layer neural network with multiple nodes where each node accepts multiple inputs and generates one output. It consists of a weight, a bias and a summation function. In the learning phase the weights are adjusted according to the weighted sum of the inputs (the net).

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1)The Adaline Algorithm:

Steps:

1. Weights and bias are set to some random fraction values but not to zero. Set the learning rate  $\alpha$ .
2. Perform steps 3 to 7 till the stopping condition is false
3. Perform steps 4 to 6 for each bipolar training pair(s:t)
4. The input layer containing the input units is applied with activation function  $x_i=s_i$
5. Calculate the net input to output of the network

$$Y_{in} = b + \sum x_i w_i$$

where  $i=1$  to  $n$  and  $n$  is the number of input neurons at input layer.

Apply the activation function

$$Y = f(y_{in}) = \begin{cases} 1 & \text{if } y_{in} > \theta \\ 0 & \text{if } y_{in} = \theta \\ -1 & \text{if } y_{in} < \theta \end{cases}$$

6. Update the weights and bias

$$w_i(\text{new}) = w_i(\text{old}) + \alpha (t - y_{in}) x_i$$

$$b_i(\text{new}) = b_i(\text{old}) + \alpha (t - y_{in})$$

7. Train the network until there is no weight change. This is the stopping condition for the network. If it is not met then start again from step number 2.

B) THE MADALINE (Multiple Adaptive Linear Neuron )

It is a three-layer (input, hidden, output), fully connected, feed-forward artificial neural network architecture for classification that uses ADALINE units in its hidden and output layers, i.e. its activation function is the sign function. More than one adaline forms the resultant network.

$X_1$  and  $x_2$  are the two input neurons connected with the neurons in the hidden layer  $z_1$  and  $z_2$  the result of this network represented in the form of observed output(y).  $z_1$  and  $z_2$  represent output at the hidden layer connected with the bias  $b_1$  and  $b_2$ . Similarly bias  $b_3$  is connected with  $y$ . The network is combination of static and dynamic approach. The second part of network is static thus by reducing its weighted bias less by 50%.

1)The Madaine Algorithm:

Steps:

1. Weights and bias are set to some random fraction values but not to zero. Set the learning rate  $\alpha$ .
2. Let  $v_1 = v_2 = b_3 = 0.5$
3. Perform steps 3 to 9 till the stopping condition is false
4. Perform steps 4 to 8 for each bipolar training pair(s:t)
5. The input layer containing the input units is applied with activation function  $x_i=s_i$
6. Calculate the net input to output at hidden layer of the network

$$Z_{in1} = b_1 + x_1 w_{11} + x_2 w_{21}$$

$$Z_{in2} = b_2 + x_1 w_{12} + x_2 w_{22}$$

Apply the activation function

$$Z_1 = f(z_{in1}) = \begin{cases} 1 & \text{if } z_{in1} > \theta \end{cases}$$

$$Z_2 = f(z_{in2}) = \begin{cases} -1 & \text{if } z_{in1} \leq \theta \\ 1 & \text{if } z_{in2} > \theta \\ -1 & \text{if } z_{in2} \leq \theta \end{cases}$$

7. Calculate the actual output

$$Y_{in} = b_3 + z_1 v_1 + z_2 v_2$$

where n is the number of input neurons at input layer.

Apply the activation function

$$Y = f(y_{in}) = \begin{cases} 1 & \text{if } y_{in} > \theta \\ -1 & \text{if } y_{in} \leq \theta \end{cases}$$

8. Find the error and update the weights and bias

If  $t=y$ , then

$$w_{ij}(\text{new}) = w_{ij}(\text{old})$$

$$b_j(\text{new}) = b_j(\text{old})$$

else if  $t \neq y$ , then

if  $(t=1)$  then,

$$w_{ij}(\text{new}) = w_{ij}(\text{old}) + \alpha (1 - z_{ini}) x_i$$

$$b_i(\text{new}) = b_i(\text{old}) + \alpha (1 - z_{ini})$$

else if  $(t = -1)$  then,

$$w_{ij}(\text{new}) = w_{ij}(\text{old}) + \alpha (-1 - z_{ini}) x_i$$

$$b_i(\text{new}) = b_i(\text{old}) + \alpha (-1 - z_{ini})$$

9. Train the network until there is no weight change. This is the stopping condition for the network. If it is not met then start again from step number 2.

### C) The Hebb's Network

The Hebb rule determines the change in the weight connection from  $u_i$  to  $u_j$  by  $Dw_{ij} = r * a_i * a_j$ , where  $r$  is the learning rate and  $a_i, a_j$  represent the activations of  $u_i$  and  $u_j$  respectively. Thus, if both  $u_i$  and  $u_j$  are activated the weight of the connection from  $u_i$  to  $u_j$  should be increased.

1) The Hebb's Algorithm:

Steps:

1. Initialize the weights. Initially they have to be set to zero;  $w_i=0, b_i=0$ ,  $n$  is the number of input patterns.
2. Steps 3 to 5 have to be performed for each training vector and target output pair  $(s:t)$
3. Input unit activations are set  $x_i=s_i$
4. Output unit activations are set to  $y=t$
5. Adjust the weights.

$$w_i(\text{new}) = w_i(\text{old}) + x_i \cdot y$$

6. Update the bias

$$b_i(\text{new}) = b_i(\text{old}) + y$$

## IV. EXPERIMENTAL RESULTS

### Adaline Network

Enter the value for  $x_1$  &  $x_2$

1 1  
 1 -1  
 -1 1-1 -1

The result of weights is

x1	x2	y	t	dw1	dw2	db	w1	w2	b	(t-y)^2
1	1	0.600	-1.6	-0.32	-0.32	-0.32	-0.12	-0.12	-0.12	2.560
1	-1	-0.12	1.12	0.224	-0.22	0.224	0.103	-0.34	0.103	1.254
-1	1	-0.34	-0.65	0.131	-0.13	-0.13	0.235	-0.47	-0.02	0.430
-1	-1	0.212	-1.21	0.242	0.242	-0.24	0.477	-0.23	-0.26	1.470

The sum of (t-yin)^2 is5.715

1	1	-0.02	-0.97	-0.19	-0.19	-0.19	0.282	-0.42	-0.46	0.951
1	-1	0.245	0.754	0.150	-0.15	0.150	0.433	-0.57	-0.31	0.569
-1	1	-1.32	0.326	-0.06	0.065	0.065	0.368	-0.51	-0.24	0.106
-1	-1	-0.10	-0.89	0.179	0.179	-0.17	0.547	-0.33	-0.42	0.803

The sum of (t-yin)^2 is8.145

1	1	-0.21	-0.78	-0.15	-0.15	-0.15	0.390	-0.49	-0.58	0.617
1	-1	0.296	0.703	0.140	-0.14	0.140	0.531	-0.63	-0.44	0.494
-1	1	-1.60	0.607	-0.12	0.121	0.121	0.409	-0.51	-0.32	0.369
-1	-1	-0.22	-0.77	0.155	0.155	-0.15	0.565	-0.35	-0.47	0.604

The sum of (t-yin)^2 is10.23

1	1	-0.26	-0.73	-0.14	-0.14	-0.14	0.418	-0.50	-0.62	0.535
1	-1	0.295	0.704	0.140	-0.14	0.140	0.559	-0.64	-0.48	0.496
-1	1	-1.68	0.685	-0.13	0.137	0.137	0.422	-0.50	-0.34	0.470
-1	-1	-0.26	-0.73	0.147	0.147	-0.14	0.569	-0.35	-0.49	0.541

The sum of (t-yin)^2 is12.27

1	1	-0.28	-0.71	-0.14	-0.14	-0.14	0.426	-0.50	-0.63	0.515
1	-1	0.290	0.709	0.141	-0.14	0.141	0.568	-0.64	-0.49	0.503
-1	1	-1.70	0.707	-0.14	0.141	0.141	0.426	-0.50	-0.35	0.499
-1	-1	-0.27	-0.72	0.144	0.144	-0.14	0.570	-0.35	-0.49	0.520

The sum of (t-yin)^2 is14.31

1	1	-0.28	-0.71	-0.14	-0.14	-0.14	0.427	-0.50	-0.64	0.510
1	-1	0.287	0.712	0.142	-0.14	0.142	0.570	-0.64	-0.49	0.507
-1	1	-1.71	0.712	-0.14	0.142	0.142	0.427	-0.50	-0.35	0.507
-1	-1	-0.28	-0.71	0.143	0.143	-0.14	0.571	-0.35	-0.49	0.513

The sum of (t-yin)^2 is16.35

- 2.430
- 2.085
- 2.044
- 2.039
- 2.039

## Madaline Network

Enter value for x1 and x2

```
1    1
1    -1
-1   1
-1   -1
```

x1	x2	t	Zin1	Zin2	Z1	Z2	Yin	Y	W11	W21	b1	W12	W22	b2
1	1	-1	0.55	0.45	1	1	1.5	1	-0.725	-0.524	-0.475	-0.675	-0.524	-0.575
1	-1	1	-0.675	-0.725	-1	-1	-0.5	-1	0.1125	-1.387	0.3625	0.1624	-1.387	0.2875
-1	1	1	-1.137	-1.262	-1	-1	-0.5	-1	-0.956	-0.256	1.4312	-0.906	-0.256	1.4187
-1	-1	-1	2.6437	2.5812	1	1	1.5	1	0.8656	1.5343	-0.390	0.9156	1.5343	-0.371

## Hebb's Network

### ANDNOT

Enter value for x1 and x2

```
1    1
1    -1
-1   1
-1   -1
```

The final output

x1	x2	y	dw1	dw2	db	w1	w2	b
1	1	-1	-1	-1	-1	-1	-1	-1
1	-1	1	1	-1	1	0	-2	0
-1	1	-1	1	-1	-1	1	-3	-1
-1	-1	-1	1	1	-1	2	-2	-2

## V. CONCLUSION

The Essential requirement of Artificial Neural Networks is to test the response of the neurons. The experimental results shows that MADALINE has good features regarding the response of the neurons because it is a combination of multiple ADALINE networks.

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